

# GROUND STATE SOLUTIONS FOR THE COUPLED KLEIN-GORDON AND MAXWELL EQUATIONS

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In this work we study the coupled Klein-Gordon and Maxwell equations when the nonlinearity exhibits critical growth. We prove the existence of ground state solutions when a potential  $V$  is introduced. The main feature of this kind of problem is the lack of compactness arising in connection with the use of variational methods.

## References

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